

# Implementation of Self-Bending Airborne Ultrasonic Beam with a Reflector for Phase-Coded Modulation

反射板を利用した位相符号化制御による  
空中超音波ビームベンディングの実装

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## 1. Introduction

Acoustic self-bending beam is an appealing phenomenon, which can generate a beam supernaturally along a curving trajectory [1]. Particularly, the beam bending for airborne ultrasound has a large expectation for some applications requiring control of sound fields such as audible area control for parametric loudspeakers [2].

A method for generating a self-bending ultrasonic beam in air is the phase-coded modulation which translates the Airy function into an initial spatial phase distribution in the binary form expressed by 0 and  $\pi$  [3]. The self-bending airborne ultrasonic beam based on the Airy function has been implemented approximately by controlling the amplitude of the sound source in binary, instead of the phase [2]. However, it makes numerous sidelobes aside from bending the main lobe, resulting in a weak convergence of sound pressure into the main lobe. Hence, it is required to invent another way to implement the phase-coded modulation in order to utilize the self-bending airborne ultrasonic beam as a basis for certain applications.

In this study, we propose a new method that adjusts the spatial phase distribution of sound waves with the reflector for implementing a self-bending airborne ultrasonic beam. We designed the reflector based on the phase-coded modulation, fabricated with a universal 3D printer and experimentally evaluated the sound field when with the manufactured reflector.

## 2. Methodology

### 2.1. Explanation of phase-coded modulation

A spatial phase pattern for the design of the reflector was determined based on the phase-coded modulation. First, it is assumed that  $\Phi(u) = \text{Ai}(bu)e^{au}$ , where  $\text{Ai}(bu)$  is the Airy function [3]. Here, the spatial phase distribution  $\theta(u)$  derived from  $\Phi(u)$  is defined as 0 and  $\pi$ , for  $\Phi(u) < 0$  and  $\Phi(u) > 0$ , respectively [3].

### 2.2. Design of a reflector

The phase was adjusted by using a reflector as described in Fig. 1. The difference in the distance that sound waves would reach the virtual radiating surface from the sound source through each path  $P_A$  and  $P_B$  is  $d/\cos \alpha$ , where  $\alpha$  is the incident

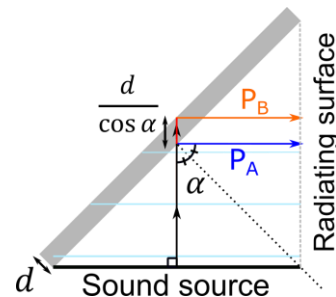
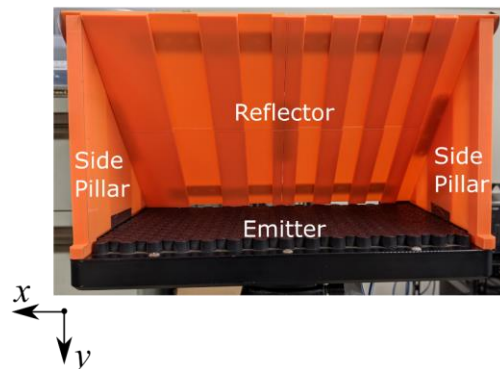
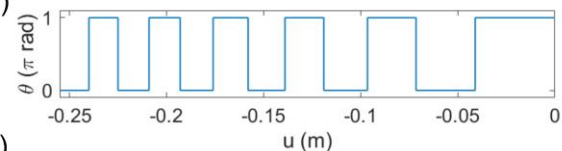


Fig. 1 The diagram for explanation of phase delay.

(a)



(b)



(c)

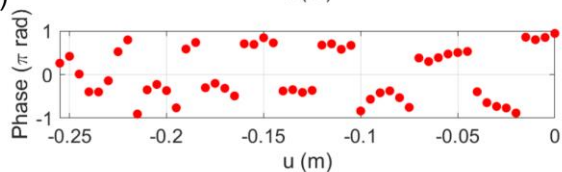


Fig. 2 (a) The fabricated reflector mounting with the emitter. (b) The spatial phase distribution that was designed and (c) measured the manufactured reflector.

angle and  $d$  is the thickness of the reflector. If the phase difference of the two sound waves on the radiating surface is equal to  $\pi$ , then the difference  $d/\cos \alpha$  is equal to  $\lambda/2$  where  $\lambda$  is the wavelength.

A reflector was designed for  $d = 3$  mm,  $\alpha = 45^\circ$ , frequency  $f = 40$  kHz and the sound speed  $c = 340$  m/s, and verified theoretically and experimentally.

Next, we implemented the phase shifter by setting steps whose height is 3 mm on the reflector

for the position corresponding to the areas whose  $\theta = \pi$  rad in the spatial phase distribution and no steps to the areas of 0 rad. We performed 3D printing to manufacture the reflector depicting the same pattern as  $\Phi(u)$ , expressing with the steps of 3 mm. We determined the spatial phase distribution based on the phase-coded modulation with parameters  $a = 1 \text{ m}^{-1}$ ,  $b = 57 \text{ m}^{-1}$  in  $\Phi(u)$ , and with the total length of 255 mm to fit the ultrasonic emitter we used for experiments.

The fabricated reflector is shown in **Fig. 2(a)**. In order to keep the incident angle stable, side pillars were mounted on both sides of an ultrasonic emitter.

### 2.3 Evaluation of the reflector

We examined the spatial phase distribution of the reflector by scanning a microphone along the  $x$ -axis perpendicular to the radiational direction of the emitter and the range direction  $z$  on the radiation surface. **Figures 2(b) and (c)** show the initial phase distribution  $\theta$  designed in Chap. 2.2 and the phase distribution measured in the experiment. This result proves that the manufactured reflector reflects the incoming waves with shifts in their phase as designed.

## 3. Evaluation of the sound field

### 3.1 Preparation

We observed the sound field when mounting the reflector on the emitter. The block diagram of the experimental setting is shown in **Fig.3**. The driving frequency of the emitter was 40 kHz. The sound pressure was measured by traversing a microphone in the sound field.

Also, we demonstrated the sound field with FEM in 2D for the configuration that a sound source has the spatial phase distribution described in Fig.2(b) [2]. For simulation, the driving frequency was set same value as the experiment. The pressure amplitude of the sound source was set to 1 Pa. The sound source was located along the  $x$ -axis, perpendicular to the range direction  $z$ -axis. Sommerfeld radiation condition was applied as the outer boundary condition [2].

### 3.2 Results and Discussions

The sound pressure level (SPL) measured on the sound field is plotted in **Fig. 4**. Each figure describes the results for each distance from the emitter. It can be seen that the SPL for when with reflector has a peak at  $(x, z) = (12.5 \text{ cm}, 0.4 \text{ m})$  and the peak shifts to the direction of increasing  $x$  as the distance getting further, resulting in the peak at  $(x, z) = (22.5 \text{ cm}, 1.0 \text{ m})$ . Apart from the slight discordance of the peaks' position, this measurement agrees with the result of the simulation. This result shows that the proposed method could generate a self-bending main lobe with 40 kHz-ultrasound in air.

## 4. Conclusion

A method for implementing a self-bending ultrasonic beam in air, which uses a reflector that was

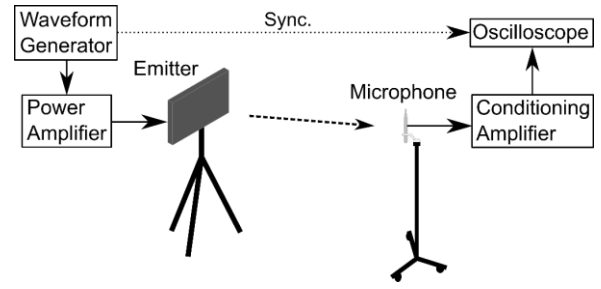


Fig. 3 The diagram of the experimental setup.

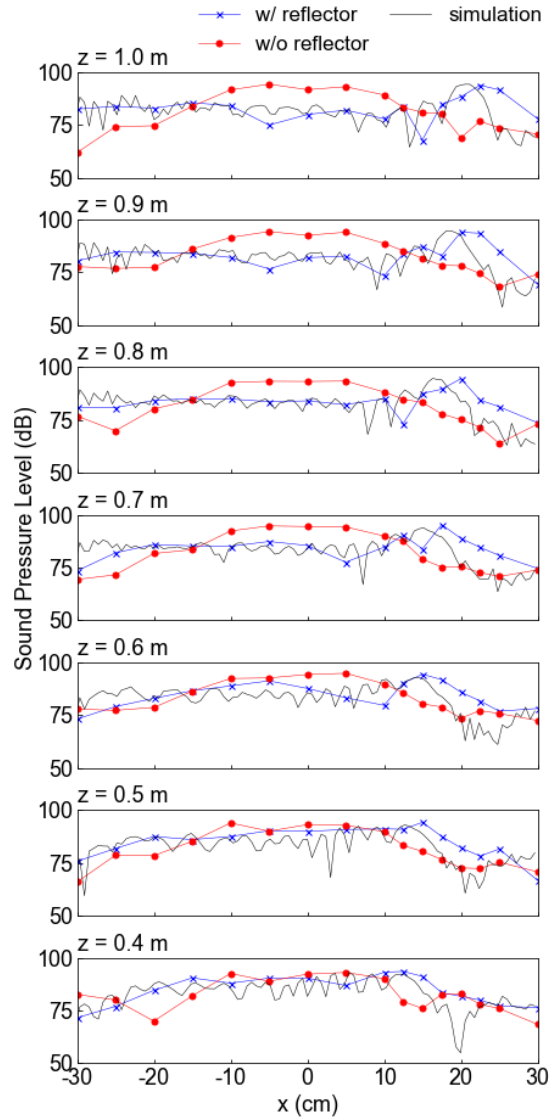


Fig. 4 The sound pressure level of the field.

designed based on phase-coded modulation and was easily fabricated, was proposed in this study. It is experimentally proven that the proposed method can generate the self-bending airborne ultrasonic beam.

## References

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